COMS W3101-2

## Programming Languages: MATLAB

## Lecture 1

Spring 2010
Instructor: Michele Merler

## Course Information - Instructor

- Michele Merler
- Email: mmerler@cs.columbia.edu
- Office : 624 CEPSR
- Office Hours: TDB
- $3^{\text {rd }}$ year PhD Student in CS Department
- Research Interests:
- Image \& Video Processing
- Multimedia
- Computer Vision


## Course Information - TA

- Daniel Miau
- Email: dm2701@columbia.edu
- Office : TA room
- Office Hours: Mon 10am - 12pm
- Rohit Sethi
- Email: rs2990@columbia.edu
- Office: TA room
- Office Hours: Wed 3.30pm - 5.30pm


## Course Information - Goals

Learn how to use MATLAB for:

- Solve problems in Science and Engineering
- Perform Matrix and Vector Operations
- Compute Complex Mathematical Functions
- Plotting and Visualization
- Perform Simulations and Prototyping


## Course Information - Syllabus

- Week 1 - March 2
- Data Structures (Variables, Vectors, Matrices)
- Types (int, double, single)
- Operators
- Basic Plotting
- Scripts
- Week 2 - March 9
- Plotting (continued)
- Control flow (if_else, for, while, loops)


## Course Information - Syllabus

- Week 3 - March 16 March 23
- I/O (from files, images, loading/saving variables)
- User input
- Advanced data structures (cell, struct)
- Debugging
- Functions
- Week 4 - March 30
- Figures
- Images
- Videos


## Course Information - Syllabus

- Week 5 - April 6
- Math and Linear Algebra
- Solving Equations, basic statistics
- Week 6 - April 13
- Final Useful things
- Object Oriented Programming
- GUI
- Simulink \& other Toolboxes


## Course Information - Grading

- 5 Homeworks ( $15 \%, 15 \%, 15 \%$, $15 \%$, $15 \%$ )
- 1 Midterm Quiz (25\%) In class March. 30



## Technical Details

- Download Xming and Putty (for Windows)
- http://sourceforge.net/projects/xming/
- http://www.chiark.greenend.org.uk/~sgtatham/put ty/download.html


## Technical Details

- Launch Xming
- Open a session in putty with Host Name - cunix.cc.columbia.edu



## Technical Details

## - Make sure the X1 1 option of the SSH category is enabled



## Technical Details

- Enter your cunix credentials
- Type
- \$ matlab \&


## What is MATLAB?

- Programming Environment
- Calculator
- Programming Language
- The solution to all your problems


## What is MATLAB?

MATLAB ${ }^{\circledR}$ is a high-level language and interactive environment that enables you to perform computationally intensive tasks than with traditional programming languages such as C, C++, and Fortran
http://www.mathworks.com/products/matlab/

## What can you do with Matlab?

- Design
- Compute
- Visualize


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## MATLAB Interface



## Basics

- MATLAB records in the workspace and command history everything you write in the command window, so:
- clear variable
- deletes variable from memory (and workspace)
- clear all
- deletes all variables from memory (and workspace)
- clc
- cleans command window


## Basics

- MATLAB's command window works like a Linux terminal
- Some example commands:
- cd
- mkdir, rmdir
- ls


## Basics

- Some commands used to interact with MATLAB
- what
- returns the MATLAB files (.m , .mat) in the current directory
- who
- returns the variables in your workspace
- whos
- returns the variables in the workspace with additional info (size, dimensions)


## Help <br> Meet your best friend...

- Start $\mapsto$ Help
- Press ? in interface


Type doc name_function
... what about help name_function ?

## Data Structures - Variables

- MATLAB does not use explicit type initialization like other languages
- Just assign some value to a variable name, and MATLAB will automagically understand its type
- int $x$
- $x=3$
- $x=$ 'hello'

- We can assign mathematical expressions to directly create variable - $x=(3+4) / 2$
- ; operator prevents the variable to be printed in the command window
- $\mathrm{x}=3$;
- disp prevents ans= from being displayed - disp(x)


## Data Structures - Variables

- MATLAB does not use explicit type initialization like other languages
- Just assign some value to a variable name, and MATLAB will automagically understand its type
- DKx
$\therefore x=3$
- $x=$ 'hello'

- We can assign mathematical expressions to directly create variable - $x=(3+4) / 2$
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## Data Structures - Variables

- Naming Conventions
- Letter case matters
$A=2$
$a=4$$\longrightarrow$ These are 2 different variables!
- Avoid using functions names for variables

- Built-in Variables
- i and $j$ indicate complex numbers

。 $\mathrm{pi}=3.1415926 \ldots$

- ans = last unassigned value
- Inf and -Inf = positive and negative infinity
- NaN = 'Not a Number'


## Data Structures - Arrays and Matrices

- This is really what MATLAB is all about!
- Row vectors
$\therefore r=[2357] ;$
$\circ r=[2, ~ 3, ~ 5, ~ 7] ;$
Column vectors
- c = [2; 3; 5; 7];
$\circ=\left[\begin{array}{llll}2 & 3 & 5 & 7\end{array}\right]$;
Transpose operator
[1×4]

| 2 | 3 | 5 | 7 |
| :--- | :--- | :--- | :--- |

[4×1] | 2 |
| :---: |
|  |

## Data Structures - Vectors

- Special Vectors Constructors
- : operator
- $\mathrm{x}=1: 3: 13$;

Spacing, default = 1

$$
[1 \times 5]
$$

| 1 | 4 | 7 | 10 | 13 |
| :--- | :--- | :--- | :--- | :--- |

- linspace()
- x = linspace(0,10,100);

Creates a vector of 100 elements with values equally spaced between 0 and 10 (included)

- Equivalent notation with : operator?


## Data Structures - Matrices

- Explicit Definition

$$
\text { - } M=[24 ; 36 ; 8 \text { 12]; }
$$

- Concatenation of vectors

| $[3 \times 2]$ | 2 | 4 |
| :---: | :---: | :---: |
|  | 3 | 6 |
| 8 | 12 |  |

- $r 1=\left[\begin{array}{ll}2 & 4]\end{array}\right.$
- $r 2=\left[\begin{array}{ll}3 & 6] ;\end{array}\right.$
- $r 3=\left[\begin{array}{ll}8 & 12] ;\end{array}\right.$
- $M=[r 1 ; r 2 ; r 3] ;$
- Concatenation of vectors and matrices
- $r 1=$ [2 4];
- $\mathrm{m} 1=[3$ 6; 8 12];
- $M=[r 1 ; \mathrm{m} 1]$;


## Data Structures - Matrices

## - Some Predefined Matrix Creation Functions

$$
\left(\begin{array}{c}
\circ \mathrm{M}=\operatorname{zeros}(2,3) ; \quad[3 \times 2] \text { matrix of zeros } \\
\text { rows columns }
\end{array}\right.
$$

| 0 | 0 | 0 |
| :--- | :--- | :--- |
| 0 | 0 | 0 |

- $M=$ ones $(2,3)$; $\quad$ [3x2] matrix of ones

| 1 | 1 | 1 |
| :--- | :--- | :--- |
| 1 | 1 | 1 |

$$
\text { - } M=\text { eye ( } 2 \text { ); [2x2] identity matrix }
$$

- $M=\operatorname{rand}(2,3) ; \quad[2 \times 3]$ matrix of uniformly distributed random numbers in range $[0,1]$

| 0.2 | 0.86 | 0.1 |
| :---: | :---: | :---: |
| 1 | 0 | 0.33 |

- $\mathrm{M}=\operatorname{randn}(2,3)$
[2x3] matrix of normally distributed random numbers (mean 0 , std dev. 1)

| -1.2 | -0.86 | 0.1 |
| :---: | :---: | :---: |
| 1.256 | 0.435 | -1.33 |

## Data Structures - Matrices

- Replicating and concatenating matrices
- repmat

X | 1 | 2 | 3 |
| :--- | :--- | :--- |
| 4 | 5 | 6 |

- $X=[123 ; 456] ;$
- $Y=\operatorname{repmat}(X, 2,4)$;
- vertcat
- $\mathrm{x} 1=\left[\begin{array}{ll}2 & 3\end{array}\right]$;
- $x 2=\left[\begin{array}{ll}1 & 2\end{array}\right] ;$
- X = vertcat(x1,x2);
- horzcat

$$
\begin{aligned}
& \cdot x 1=[2 ; 3 ; 4] ; \\
& \cdot x 2=[1 ; 2 ; 3] ; \\
& \text { - } x=\operatorname{horzcat}(x 1, x 2) ;
\end{aligned}
$$

$$
\begin{array}{|l|l|}
\hline x 1 & 2 \\
\hline 3 \\
\hline 4 \\
\hline 4 \\
\hline
\end{array} \quad \begin{array}{|l|l|l|}
\hline 1 \\
\hline 2 \\
\hline 3 \\
\hline
\end{array} \quad \begin{array}{|c|c|}
\hline 2 & 1 \\
\hline 3 & 2 \\
\hline 4 & 3 \\
\hline
\end{array}
$$

## Data Structures - Matrices

-Getting the size of the matrix

$$
\begin{aligned}
& \text { - } M=\left[\begin{array}{llll}
2 & 3 & 4 & 3
\end{array}\right. \text { 55]; } \\
& \text { - [r c] = size(M); } \\
& \text { - } r=\operatorname{size}(M, 1) \text {; } \\
& r=2 ; \\
& \text { - c = size (M, 2) ; } \\
& \text { c }=3 \text {; }
\end{aligned}
$$

## Data Structures - Matrices

- Accessing Elements of Matrix M
- Matrix indexing starts with 1!
- Explicit access
- element $=\mathrm{M}(2,3)$;
- element $=$ M(5);
- : operator

M | -1.2 | -0.86 | 0.1 |
| :---: | :---: | :---: |
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- element $=$ M(1,1:2);
- element $=\mathrm{M}(:, 1)$;
- end operator
- element $=$ M(1,2:end);


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- element $=M(:, 1)$;
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- element $=$ M(1,1:2);
- element $=\mathrm{M}(:, 1)$;
- end operator
- element $=M(1,2$ :end);


## Types

$\begin{array}{|l|c|l|}\hline \text { Type name } & \text { bits } & \text { Example } \\ \hline \text { double } & 64 & \mathrm{x}=32 \\ \hline \text { char } & 16 & \mathrm{x}=\text { 'as' } \\ \hline \text { (u)int8 } & 8 & \mathrm{x}=(\mathrm{u}) \text { int8(32) } \\ \hline \text { (u)int16 } & 16 & \mathrm{x}=(\mathrm{u}) \text { int16(32) } \\ \hline \text { (u)int32 } & 32 & \mathrm{x}=(\mathrm{u}) \text { int32(32) } \\ \hline \text { (u)int64 } & 64 & \mathrm{x}=(\mathrm{u}) \text { int64(32) } \\ \hline \text { single float } & 32 & \mathrm{x}=\text { single(32) } \\ \hline \text { complex } & 128(64+64) & \mathrm{x}=\text { complex(2,1) } \\ \hline \text { logical } & 1 & \mathrm{x}=\text { true, } \mathrm{x}=\text { logical([ll } 0 \\ \hline\end{array}$ 1] $]$

- Note on complex numbers:

```
。 \(x=3+4 j ;\)
- \(\mathrm{x}=\) complex \((3,4)\);
```


## Operators

- Basic Mathematical Operators
-     +         -             * / ^
- Some more complex mathematical functions

```
- sqrt()
- log(), exp()
- sin(), cos(), tan(), atan()
- abs(), angle()
- round(), floor(), ceil()
- conj(), imag(), real()
- sign()
```

- Logical Operators
- Relational Operators
$\circ \gg=<=$


## Operators

- Operators on matrices
- $X=\left[\begin{array}{lllll}2 & 3 & 4 ; & 4 & 6\end{array}\right] ;$
- $Y=\left[\begin{array}{lllll}1 & 2 & 3 ; & 3 & 3\end{array}\right]$;
- Rplus $=\mathrm{X}+\mathrm{Y}$;
- Rminus = X - Y;

Rplus | 3 | 5 | 7 |
| :--- | :--- | :--- |
| 8 | 7 | 9 |

- Rmult $=\mathrm{X} * \mathrm{Y}$; ??? Error using $==>$ mtimes

| Rminus | 1 | 1 | 1 |
| :--- | :--- | :--- | :--- |
|  | 1 | 1 | 3 |
|  | 2 | 1 |  |
|  |  |  |  |

- $\mathrm{X} 2=\mathrm{X}^{\prime}$; agree.
- Rmult $=\mathrm{X} 2$ * Y ;

Rmult | 4 | 9 | 16 |
| :---: | :---: | :---: |
| 25 | 16 | 36 |

- Rpoint_mult $=\mathrm{X} . * \mathrm{Y}$;

Rpoint_mult

| 2 | 6 | 12 |
| :---: | :---: | :---: |
| 15 | 12 | 18 |

Some operators, like + and - , are always element wise !
Other operators, like $*$ and /, must be disambiguated with . !

## Operators

- Operators on matrices

$X$| 2 | 3 | 4 |
| :---: | :---: | :---: |
| 5 | 4 | 6 |


| 1 | 2 | 3 |
| :---: | :---: | :---: |
| 3 | 3 | 3 |

- $\mathrm{R}=\mathrm{X}$ ^ 2 ??? Error using ==> mpower
${ }^{\circ}=X \wedge 2$ Matrix must be square
- $\mathrm{X} 2=\left[\begin{array}{lllll}1 & 2 & 3 ; & 4 & 5 ; \\ 1 & 1\end{array}\right]$;
- Rsquare $=\mathrm{X} 2$ ^ 2;

X2 | 1 | 2 | 3 |
| :---: | :---: | :---: |
| 3 | 4 | 5 |
| 1 | 1 | 1 |

Rsquare $=$\begin{tabular}{|c|c|c|}
\hline 1 \& 2 \& 3 <br>
\hline 3 \& 4 \& 5 <br>
\hline 1 \& 1 \& 1 <br>
\hline

$*$

\hline 1 \& 2 \& 3 <br>
\hline 3 \& 4 \& 5 <br>
\hline 1 \& 1 \& 1 <br>
\hline

$=$

\hline 10 \& 13 \& 16 <br>
\hline 20 \& 27 \& 34 <br>
\hline 5 \& 7 \& 9 <br>
\hline
\end{tabular}

- Rdot $=\mathrm{X} . \wedge 2$

Rdot

| 4 | 9 | 16 |
| :---: | :---: | :---: |
| 25 | 16 | 36 |

## Operators

- Special Functions for Matrices

```
- sum(),prod()
    - SumCols = sum(X);
    - SumRows = sum(X,2);
    - SumTot = sum(sum(X));
```

- mean ()
    - MeanCols $=$ mean(X);
    - MeanRows $=$ mean(X,2);
    - MeanTot $=$ mean(mean(X)); MeanTot $=3.5$
- max(), min()
- MaxVal = max(max(X));
- minCols $=\min (X)$;
- minRows $=[\min (X(1,:)) ; \min (X(2,:))] ;$ minRows

$$
\text { MaxVal }=6
$$

- minCols $=\min (X)$;
$\square$
- minRows2 $=\min (X, 2) \equiv \min (X, 2 *$ ones $(\operatorname{size}(X)))$
$\min \left(\begin{array}{|l|l|l|}\hline 1 & 2 & 3 \\ \hline 4 & 5 & 6 \\ \hline\end{array}\right.$

| 2 | 2 | 2 |
| :--- | :--- | :--- |
| 2 | 2 | 2 |$\rightarrow$| 1 | 2 | 2 |
| :--- | :--- | :--- |
| 2 | 2 | 2 |

## Operators

$$
\begin{aligned}
& \mathrm{X}=\left[\begin{array}{lllll|l|l|l|}
1 & 2 & 13 & 4 & 5 & 6
\end{array}\right] ; \\
& \mathrm{X} \begin{array}{|l|l|l|l|l|l|l|}
\hline 1 & 2 & 13 & 4 & 5 & 6 \\
\hline
\end{array}
\end{aligned}
$$

- Special Functions for Matrices
- max(), min() - continued
- [maxVal maxLoc] $=\max (X) ; \quad \operatorname{maxVal}=13$, maxLoc $=3$ MATLAB also tells us the location of the maximum value!
- sort() - orders the elements of a vector in ascending (default) or descending order
- xAsc = sort(X);

| xAsc | 1 | 2 | 4 | 5 | 6 | 13 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| xDes | 13 | 6 | 5 | 4 | 2 | 1 |
| order | 3 | 6 | 5 | 4 | 2 | 1 |

- find()

$$
\begin{aligned}
& \text { - } R=\text { find }(X>4) \text {; } \\
& \begin{array}{l|l|l|l|}
\hline 3 & 5 & 6 \\
\hline
\end{array} \\
& \text { - } R=\text { find }(X==13) \text {; } \\
& \mathrm{R}=3 \\
& \mathrm{X}=[1213 ; 456] ; \\
& \text { - } R=\text { find }(X>=2 \& X<6)^{\prime} ; \\
& \text { - }\left[\begin{array}{ll}
r & c
\end{array}\right]=\operatorname{find}(X=6) \text {; } \\
& \text { - } R=\text { find }(X>=2 \& X<6)^{\prime} ; \\
& {\left[\begin{array}{ll}
r & c
\end{array}\right]=\operatorname{find}(X=6) \text {; }} \\
& r=2 \quad c=3
\end{aligned}
$$

## Matrix indexing

- If we want to define the position of element 1 within the matrix M , we can do it with a single index or with the indexes of row and column

$$
\begin{aligned}
& \circ M=[24 ; 36 ; 51 ; 812] ; \\
& \text { - index }=\text { find }(M==1) ;
\end{aligned}
$$

|  | $M$ |
| :---: | :---: |
| 2 | 4 |
| 3 | 6 |
| 5 | 1 |
| 8 | 12 |

- ind2sub
- [r c] = ind2sub(size(M),index);
- sub2ind
- newIndex $=$ sub2ind(size(M),r,c);


## Matrix indexing

- If we want to define the position of element 1 within the matrix M , we can do it with a single index or with the indexes of row and column

```
- \(M=[24 ; 36 ; 51 ; 812] ;\)
- index \(=\) find ( \(M==1\) );
                7
```

|  | $M$ |
| :---: | :---: |
| 2 | 4 |
| 3 | 6 |
| 5 | 1 |
| 8 | 12 |

- ind2sub

```
- [r c] \(=\) ind2sub(size(M),index);
        32
```

        It's necessary to provide
    - sub2ind the size of the matrix!
- newIndex $=$ sub2ind(size(M),r,c);


## Basic Plotting

plot()

- $x=[-1: 0.1: 1] ;$
${ }^{\circ} \mathrm{y}=\mathrm{x} . \wedge 2$;
- plot(y) ;
- plot(x,y) ;




## Basic Plotting

plot()

- $x=$ [-1:0.1:1];
- $y=x . \wedge 2 ;$
- plot(y);
- plot(x,y);


© plot(x,y,'--rd','LineWidth',2,... 'MarkerEdgeColor', 'b' , . .
 'MarkerFaceColor','g',... 'MarkerSize',10);


## Basic Plotting

- plot()
- $x=$ [-1:0.1:1];
- $y=x . \wedge 2 ;$
- plot(y);
- plot(x,y);


© plot(x,y,'--rd','LineWidth',2,... 'MarkerEdgeColor', 'b' , . .
'MarkerFaceColor','g',... 'MarkerSize',10);
- Line style - -
- Line color 'red'
- Marker Type 'diamond’


## Basic Plotting

- bar ()
- $x=100 * r a n d(1,20)$;
- bar(x);
- xlabel('x');
- ylabel('values');
- axis ([ $\underbrace{0}_{\text {0 range }} 21 \quad \underbrace{0}_{\text {range }} 120])$; xlim([0 21]); ylim([0 120]);
- pie()
- $x=100 *$ rand $(1,5)$;
- pie(x);
- title('My first pie!');
- legend('val1','val2',... 'val3','val4','val5');




## Basic Plotting

- figure
- To open a new Figure and avoid overwriting plots
- x = [-pi:0.1:pi];
- $y=\sin (x)$;
- $\mathrm{z}=\cos (\mathrm{x})$;

The fist plot command

- plot(x,y); automatically creates a
- figure
- plot(x,z);
- Close figures
- close 1
- close all
- Multiple plots in same Graph
- plot(x,y);
- hold on
- plot(x,z,'r');
-hold off



## Basic Plotting

- Multiple plots in same Figure
- figure(1)
- subplot(2,2,1)
- plot(x,y);
- title('sin(x)');
- subplot(2,2,2)
- plot(x,z,'r');
- title('exp(-x)');
- subplot(2,2,3)
- bar(x) ;
- title('bar(x)');
- subplot(2,2,4)
- pie(x) ;
- title('pie(x)');



## Scripts

- Like a notebook, but for code!

- M-files are MATLAB specific script files, they are called namefile.m

- You can open scripts from command window too, just type open scriptname


## Comments

- Adding comments to your code is a very healthy habit
- Think about other people who have to read and understand 3000 lines of your code!
- MATLAB comments, the \% operator
- $x=\left[\begin{array}{llll}1 & 2 & 3 & 4\end{array}\right]$
- \% this is a comment
- bar(x) ;
- title('bar(x)');
- When you type help namefunction in the command window, what you get is the comments on top of the namefunction.m script


## Homeworks policy

- Due at beginning of class, no exceptions
- Put your code (.m files) and additional files in a single folder, name it youruni_hw_ $X$ and zip it
- Upload the zipped folder to CourseWorks
- Bring a printout of your code to class


Good luck and have fun !!!

## Conclusion

- MATLAB is also a philosopher!

Try typing why in the command window... you'll get the answers!!!

