6.864 (Fall 2007): Lecture 7	INPUT: Profits soared at Boeing Co., easily topping forecasts on Wall Street, as their CEO Alan Mulally announced first quarter results. OUTPUT:
Tagging	Profits/N soared/V at/P Boeing/N Co./N ,/, easily/ADV topping/V forecasts/N on/P Wall/N Street/N ,/, as/P their/POSS CEO/N Alan/N Mulally/N announced/V first/ADJ quarter/N results/N ./. N = Noun V = Verb P = Preposition Adv = Adverb Adj = Adjective
1	2
1	3
<u>Overview</u>	Named Entity Recognition
Overview • The Tagging Problem • Hidden Markov Model (HMM) taggers	Named Entity Recognition INPUT: Profits soared at Boeing Co., easily topping forecasts on Wall Street, as their CEO Alan Mulally announced first quarter results. OUTPUT: Profits soared at [Company Boeing Co.], easily topping forecasts on [Location Wall Street], as their CEO [Person Alan Mulally] announced first
• The Tagging Problem	Named Entity Recognition INPUT: Profits soared at Boeing Co., easily topping forecasts on Wall Street, as their CEO Alan Mulally announced first quarter results. OUTPUT: Profits soared at [Company Boeing Co.], easily topping forecasts

Part-of-Speech Tagging

Named Entity Extraction as Tagging

INPUT:

Profits soared at Boeing Co., easily topping forecasts on Wall Street, as their CEO Alan Mulally announced first quarter results.

OUTPUT:

Profits/NA soared/NA at/NA Boeing/SC Co./CC ,/NA easily/NA topping/NA forecasts/NA on/NA Wall/SL Street/CL ,/NA as/NA their/NA CEO/NA Alan/SP Mulally/CP announced/NA first/NA quarter/NA results/NA ./NA

- NA = No entity
- SC = Start Company
- **CC** = Continue Company
- **SL** = Start Location
- **CL** = Continue Location
- . . .

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Our Goal

Training set:

1 Pierre/NNP Vinken/NNP ,/, 61/CD years/NNS old/JJ ,/, will/MD join/VB the/DT board/NN as/IN a/DT nonexecutive/JJ director/NN Nov./NNP 29/CD ./.

2 Mr./NNP Vinken/NNP is/VBZ chairman/NN of/IN Elsevier/NNP N.V./NNP ,/, the/DT Dutch/NNP publishing/VBG group/NN ./.

3 Rudolph/NNP Agnew/NNP ,/, 55/CD years/NNS old/JJ and/CC chairman/NN of/IN Consolidated/NNP Gold/NNP Fields/NNP PLC/NNP ,/, was/VBD named/VBN a/DT nonexecutive/JJ director/NN of/IN this/DT British/JJ industrial/JJ conglomerate/NN ./.

38,219 It/PRP is/VBZ also/RB pulling/VBG 20/CD people/NNS out/IN of/IN Puerto/NNP Rico/NNP ,/, who/WP were/VBD helping/VBG Huricane/NNP Hugo/NNP victims/NNS ,/, and/CC sending/VBG them/PRP to/TO San/NNP Francisco/NNP instead/RB ./.

• From the training set, induce a function/algorithm that maps new sentences to their tag sequences.

Two Types of Constraints

Influential/JJ members/NNS of/IN the/DT House/NNP Ways/NNP and/CC Means/NNP Committee/NNP introduced/VBD legislation/NN that/WDT would/MD restrict/VB how/WRB the/DT new/JJ savings-and-loan/NN bailout/NN agency/NN can/MD raise/VB capital/NN ./.

- "Local": e.g., *can* is more likely to be a modal verb MD rather than a noun NN
- "Contextual": e.g., a noun is much more likely than a verb to follow a determiner
- Sometimes these preferences are in conflict:

The trash can is in the garage

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A Naive Approach

- Use a machine learning method to build a "classifier" that maps each word individually to its tag
- A problem: does not take contextual constraints into account

Overview

- The Tagging Problem
- Hidden Markov Model (HMM) taggers
 - Basic definitions
 - Parameter estimation
 - The Viterbi Algorithm
- Log-linear taggers
- Log-linear models for parsing and other problems

A Trigram HMM Tagger:

 $P(T,S) = P(\text{END} \mid w_1 \dots w_n, t_1 \dots t_n) \times \prod_{j=1}^n \left[P(t_j \mid w_1 \dots w_{j-1}, t_1 \dots t_{j-1}) \times P(w_j \mid w_1 \dots w_{j-1}, t_1 \dots t_j) \right]$ Chain rule

 $= P(\text{END}|t_{n-1}, t_n) \times \\\prod_{j=1}^{n} \left[P(t_j \mid t_{j-2}, t_{j-1}) \times P(w_j \mid t_j) \right]$ Independence assumptions

- END is a special tag that terminates the sequence
- We take $t_0 = t_{-1} = *$, where * is a special "padding" symbol

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Hidden Markov Models

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- We have an input sentence $S = w_1, w_2, \dots, w_n$ (w_i is the *i*'th word in the sentence)
- We have a tag sequence $T = t_1, t_2, \ldots, t_n$ (t_i is the *i*'th tag in the sentence)
- We'll use an HMM to define

 $P(t_1, t_2, \ldots, t_n, w_1, w_2, \ldots, w_n)$

for any sentence S and tag sequence T of the same length.

• Then the most likely tag sequence for S is

$$T^* = \operatorname{argmax}_T P(T, S)$$

Independence Assumptions in the Trigram HMM Tagger

• 1st independence assumption: each tag only depends on previous two tags

 $P(t_j|w_1\dots w_{j-1}, t_1\dots t_{j-1}) = P(t_j|t_{j-2}, t_{j-1})$

• 2nd independence assumption: each word only depends on underlying tag

$$P(w_j|w_1\ldots w_{j-1}, t_1\ldots t_j) = P(w_j|t_j)$$

An Example	How to model $P(T, S)$?
• $S =$ the boy laughed	Hispaniola/NNP quickly/RB became/VB an/DT important/JJ base/Vt
• $T = DT NN VBD$	Probability of generating base/Vt:
$\begin{split} P(T,S) &= P(\text{DT} \text{START, START}) \times \\ P(\text{NN} \text{START, DT}) \times \\ P(\text{VBD} \text{DT, NN}) \times \\ P(\text{END} \text{NN, VBD}) \times \\ P(\text{the} \text{DT}) \times \\ P(\text{boy} \text{NN}) \times \\ P(\text{laughed} \text{VBD}) \end{split}$	$P(Vt \mid DT, JJ) \times P(base \mid Vt)$
13	15
Why the Name?	Overview
	Overview • The Tagging Problem
$P(T,S) = \underbrace{P(\text{END} t_{n-1}, t_n) \prod_{j=1}^{n} P(t_j \mid t_{j-2}, t_{j-1})}_{\text{Hidden Markov Chain}} \times \underbrace{\prod_{j=1}^{n} P(w_j \mid t_j)}_{w_j \text{'s are observed}}$	
$P(T,S) = \underbrace{P(\text{END} t_{n-1}, t_n) \prod_{j=1}^{n} P(t_j \mid t_{j-2}, t_{j-1})}_{j=1} \times \underbrace{\prod_{j=1}^{n} P(w_j \mid t_j)}_{j=1}$	• The Tagging Problem
$P(T,S) = \underbrace{P(\text{END} t_{n-1}, t_n) \prod_{j=1}^{n} P(t_j \mid t_{j-2}, t_{j-1})}_{j=1} \times \underbrace{\prod_{j=1}^{n} P(w_j \mid t_j)}_{j=1}$	 The Tagging Problem Hidden Markov Model (HMM) taggers
$P(T,S) = \underbrace{P(\text{END} t_{n-1}, t_n) \prod_{j=1}^{n} P(t_j \mid t_{j-2}, t_{j-1})}_{j=1} \times \underbrace{\prod_{j=1}^{n} P(w_j \mid t_j)}_{j=1}$	 The Tagging Problem Hidden Markov Model (HMM) taggers Basic definitions
$P(T,S) = \underbrace{P(\text{END} t_{n-1}, t_n) \prod_{j=1}^{n} P(t_j \mid t_{j-2}, t_{j-1})}_{j=1} \times \underbrace{\prod_{j=1}^{n} P(w_j \mid t_j)}_{j=1}$	 The Tagging Problem Hidden Markov Model (HMM) taggers Basic definitions Parameter estimation
$P(T,S) = \underbrace{P(\text{END} t_{n-1}, t_n) \prod_{j=1}^{n} P(t_j \mid t_{j-2}, t_{j-1})}_{j=1} \times \underbrace{\prod_{j=1}^{n} P(w_j \mid t_j)}_{j=1}$	 The Tagging Problem Hidden Markov Model (HMM) taggers Basic definitions Parameter estimation The Viterbi Algorithm

Smoothed Estimation

$$P(\mathbf{Vt} \mid \mathbf{DT}, \mathbf{JJ}) = \lambda_1 \times \frac{Count(\mathbf{Dt}, \mathbf{JJ}, \mathbf{Vt})}{Count(\mathbf{Dt}, \mathbf{JJ})} + \lambda_2 \times \frac{Count(\mathbf{JJ}, \mathbf{Vt})}{Count(\mathbf{JJ})} + \lambda_3 \times \frac{Count(\mathbf{Vt})}{Count(\mathbf{JJ})}$$

$$\lambda_1 + \lambda_2 + \lambda_3 = 1$$
, and for all $i, \lambda_i \ge 0$

$$P(\text{base} | \text{Vt}) = \frac{Count(\text{Vt}, \text{base})}{Count(\text{Vt})}$$

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Dealing with Low-Frequency Words

A common method is as follows:

• Step 1: Split vocabulary into two sets

Frequent words= words occurring \geq 5 times in trainingLow frequency words= all other words

• Step 2: Map low frequency words into a small, finite set, depending on prefixes, suffixes etc.

Dealing with Low-Frequency Words: An Example

[Bikel et. al 1999] (named-entity recognition)

Word class	Example	Intuition
twoDigitNum	90	Two digit year
fourDigitNum	1990	Four digit year
containsDigitAndAlpha	A8956-67	Product code
containsDigitAndDash	09-96	Date
containsDigitAndSlash	11/9/89	Date
containsDigitAndComma	23,000.00	Monetary amount
containsDigitAndPeriod	1.00	Monetary amount, percentage
othernum	456789	Other number
allCaps	BBN	Organization
capPeriod	M.	Person name initial
firstWord	fi rst word of sentence	no useful capitalization information
initCap	Sally	Capitalized word
lowercase	can	Uncapitalized word
other	,	Punctuation marks, all other words
		'
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Dealing with Low-Frequency Words: An Example

Profi ts/NA soared/NA at/NA Boeing/SC Co./CC ,/NA easily/NA topping/NA forecasts/NA on/NA Wall/SL Street/CL ,/NA as/NA their/NA CEO/NA Alan/SP Mulally/CP announced/NA fi rst/NA quarter/NA results/NA ./NA

₩

firstword/NA soared/NA at/NA initCap/SC Co./CC ,/NA easily/NA lowercase/NA forecasts/NA on/NA initCap/SL Street/CL ,/NA as/NA their/NA CEO/NA Alan/SP initCap/CP announced/NA first/NA quarter/NA results/NA ./NA

- NA = No entity
- SC = Start Company
- **CC** = Continue Company
- SL = Start Location
- **CL** = Continue Location
- ...

Overview

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The Viterbi Algorithm

• Question: how do we calculate the following?:

 $T^* = \operatorname{argmax}_T \log P(T, S)$

- Define n to be the length of the sentence
- Define a dynamic programming table
 - $\pi[i, u, v] = \max \max \log \operatorname{probability} of a tag sequence ending in tags <math>u, v$ at position i
- Our goal is to calculate

$$\max_{u,v\in\mathcal{T}}\pi[n,u,v]$$

The Viterbi Algorithm: Recursive Definitions

- Base case:
 - $\begin{aligned} \pi[0,*,*] &= & \log 1 = 0 \\ \pi[0,u,v] &= & \log 0 = -\infty \text{ for all other } u,v \end{aligned}$

here * is a special tag padding the beginning of the sentence.

• Recursive case: for $i = 1 \dots n$, for all u, v,

 $\pi[i, u, v] = \max_{t \in \mathcal{T} \cup \{*\}} \{\pi[i - 1, t, u] + Score(S, i, t, u, v)\}$

Backpointers allow us to recover the max probability sequence:

 $\text{BP}[i,u,v] \hspace{.1in} = \hspace{.1in} \operatorname{argmax}_{t \in \mathcal{T} \cup \{*\}} \left\{ \pi[i-1,t,u] + Score(S,i,t,u,v) \right\}$

Where $Score(S, i, t, u, v) = \log P(v \mid t, u) + \log P(w_i \mid v)$

Complexity is $O(nk^3)$, where n =length of sentence, k is number of possible tags

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The Viterbi Algorithm: Running Time

- $O(n|\mathcal{T}|^3)$ time to calculate Score(S, i, t, u, v) for all i, t, u, v.
- $n|\mathcal{T}|^2$ entries in π to be filled in.
- $O(\mathcal{T})$ time to fill in one entry
- $\bullet \ \Rightarrow O(n |\mathcal{T}|^3)$ time

Pros and Cons

•	Hidden markov model taggers are very simple to train
	(just need to compile counts from the training corpus)

- Perform relatively well (over 90% performance on named entities)
- Main difficulty is modeling

 $P(word \mid tag)$

can be very difficult if "words" are complex

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Overview

- The Tagging Problem
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Log-Linear Models

• We have an input sentence $S = w_1, w_2, \ldots, w_n$ $(w_i$ is the *i*'th word in the sentence) • We have a tag sequence $T = t_1, t_2, \ldots, t_n$ $(t_i \text{ is the } i)$ that tag in the sentence) • We'll use an log-linear model to define $P(t_1, t_2, \ldots, t_n | w_1, w_2, \ldots, w_n)$ for any sentence S and tag sequence T of the same length. (Note: contrast with HMM that defines $P(t_1, t_2, \ldots, t_n, w_1, w_2, \ldots, w_n))$ • Then the most likely tag sequence for S is $T^* = \operatorname{argmax}_T P(T|S)$ 27 How to model P(T|S)? A Trigram Log-Linear Tagger: $P(T|S) = \prod_{i=1}^{n} P(t_i \mid w_1 \dots w_n, t_1 \dots t_{i-1})$ Chain rule $=\prod_{i=1}^{n} P(t_{i} \mid w_{1}, \dots, w_{n}, t_{j-2}, t_{j-1})$ Independence assumptions • We take $t_0 = t_{-1} = *$ • Independence assumption: each tag only depends on previous two tags $P(t_i|w_1,\ldots,w_n,t_1,\ldots,t_{i-1}) = P(t_i|w_1,\ldots,w_n,t_{i-2},t_{i-1})$

An Example

Hispaniola/NNP quickly/RB became/VB an/DT important/JJ base/?? from which Spain expanded its empire into the rest of the Western Hemisphere .

- There are many possible tags in the position ?? $\mathcal{Y} = \{NN, NNS, Vt, Vi, IN, DT, ...\}$
- \bullet The input domain ${\cal X}$ is the set of all possible histories (or contexts)
- \bullet Need to learn a function from (history, tag) pairs to a probability P(tag|history)

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Feature Vector Representations

- We have some input domain \mathcal{X} , and a finite label set \mathcal{Y} . Aim is to provide a conditional probability $P(y \mid x)$ for any $x \in \mathcal{X}$ and $y \in \mathcal{Y}$.
- A feature is a function f : X × Y → ℝ
 (Often binary features or indicator functions f : X × Y → {0,1}).
- Say we have m features f_k for $k = 1 \dots m$ \Rightarrow A feature vector $\mathbf{f}(x, y) \in \mathbb{R}^m$ for any $x \in \mathcal{X}$ and $y \in \mathcal{Y}$.

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An Example (continued)

- \mathcal{X} is the set of all possible histories of form $\langle t_{-2}, t_{-1}, w_{[1:n]}, i \rangle$
- $\mathcal{Y} = \{NN, NNS, Vt, Vi, IN, DT, \dots\}$
- We have m features $f_k : \mathcal{X} \times \mathcal{Y} \to \mathbb{R}$ for $k = 1 \dots m$

For example:

. . .

$$f_1(h, t) = \begin{cases} 1 & \text{if current word } w_i \text{ is base and } t = \forall t \\ 0 & \text{otherwise} \end{cases}$$

$$f_2(h, t) = \begin{cases} 1 & \text{if current word } w_i \text{ ends in ing and } t = \forall \mathsf{BG} \\ 0 & \text{otherwise} \end{cases}$$

 $f_1(\langle JJ, DT, \langle Hispaniola, ... \rangle, 6 \rangle, Vt) = 1$ $f_2(\langle JJ, DT, \langle Hispaniola, ... \rangle, 6 \rangle, Vt) = 0$

Representation: Histories

- A history is a 4-tuple $\langle t_{-2}, t_{-1}, w_{[1:n]}, i \rangle$
- t_{-2}, t_{-1} are the previous two tags.
- $w_{[1:n]}$ are the n words in the input sentence.
- i is the index of the word being tagged
- \mathcal{X} is the set of all possible histories

Hispaniola/NNP quickly/RB became/VB an/DT important/JJ base/?? from which Spain expanded its empire into the rest of the Western Hemisphere .

- $t_{-2}, t_{-1} = DT, JJ$
- $w_{[1:n]} = \langle Hispaniola, quickly, became, \dots, Hemisphere, . \rangle$
- *i* = 6

The Full Set of Features in [(Ratnaparkhi, 96)]

• Word/tag features for all word/tag pairs, e.g.,

 $f_{100}(h,t) = \begin{cases} 1 & \text{if current word } w_i \text{ is base and } t = Vt \\ 0 & \text{otherwise} \end{cases}$

• Spelling features for all prefixes/suffixes of length \leq 4, e.g.,

$$\begin{array}{lll} f_{101}(h,t) &=& \left\{ \begin{array}{ll} 1 & \text{if current word } w_i \text{ ends in ing and } t = \texttt{VBG} \\ 0 & \text{otherwise} \end{array} \right. \\ f_{102}(h,t) &=& \left\{ \begin{array}{ll} 1 & \text{if current word } w_i \text{ starts with pre and } t = \texttt{NN} \\ 0 & \text{otherwise} \end{array} \right. \end{array}$$

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The Full Set of Features in [(Ratnaparkhi, 96)]

• Contextual Features, e.g.,

$$\begin{split} f_{103}(h,t) &= \begin{cases} 1 & \text{if } \langle t_{-2}, t_{-1}, t \rangle = \langle \text{DT, JJ, Vt} \rangle \\ 0 & \text{otherwise} \end{cases} \\ f_{104}(h,t) &= \begin{cases} 1 & \text{if } \langle t_{-1}, t \rangle = \langle \text{JJ, Vt} \rangle \\ 0 & \text{otherwise} \end{cases} \\ f_{105}(h,t) &= \begin{cases} 1 & \text{if } \langle t \rangle = \langle \text{Vt} \rangle \\ 0 & \text{otherwise} \end{cases} \\ f_{106}(h,t) &= \begin{cases} 1 & \text{if previous word } w_{i-1} = the \text{ and } t = \text{Vt} \\ 0 & \text{otherwise} \end{cases} \\ f_{107}(h,t) &= \begin{cases} 1 & \text{if next word } w_{i+1} = the \text{ and } t = \text{Vt} \\ 0 & \text{otherwise} \end{cases} \end{split}$$

Log-Linear Models

- We have some input domain X, and a finite label set Y. Aim is to provide a conditional probability P(y | x) for any x ∈ X and y ∈ Y.
- A feature is a function f : X × Y → ℝ
 (Often binary features or indicator functions f : X × Y → {0,1}).
- Say we have m features fk for k = 1...m
 ⇒ A feature vector f(x, y) ∈ ℝ^m for any x ∈ X and y ∈ Y.
- We also have a **parameter vector** $\mathbf{v} \in \mathbb{R}^m$
- We define

$$P(y \mid x, \mathbf{v}) = \frac{e^{\mathbf{v} \cdot \mathbf{f}(x, y)}}{\sum_{y' \in \mathcal{Y}} e^{\mathbf{v} \cdot \mathbf{f}(x, y')}}$$

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Training the Log-Linear Model

• To train a log-linear model, we need a training set (x_i, y_i) for $i = 1 \dots n$. Then search for

$$\mathbf{v}^* = \operatorname{argmax}_{\mathbf{v}} \left(\underbrace{\sum_{i} \log P(y_i | x_i, \mathbf{v})}_{Log - Likelihood} - \underbrace{\frac{1}{2\sigma^2} \sum_{k} v_k^2}_{Gaussian \ Prior} \right)$$

(see last lecture on log-linear models)

• Training set is simply all history/tag pairs seen in the training data

 Question: how do we calculate the following?: T[*] = argmax_T log P(T S) Define u to be the length of the sentence Define a dynamic programming table π[i, u, v] = maximum log probability of a tag sequence ending in tags u, v at position i Our goal is to calculate max_{u,vCT} π[n, u, v] 37 39 FAQ Segmentation: McCallum et. al (and the sentence) (b, u, v] = log 1 = 0 π[0, u, v] = log 1 = 0 π[0, u, v] = log 0 = -∞ for all other u, v here * is a special tag padding the beginning of the sentence. Recursive case: for i = 1,, n, for all u, v, π[i, u, v] = max_i {π[i - 1, t, u] + Score(S, i, t, u, v)} (corrections) (corrections) (corrections) (maximum of the maximum of the maximum of the sentence) (corrections) (maximum of the sentence) (corrections) (maximum of the sentence) (corrections) (maximum of the sentence) (maximum o	The Viterbi Algorithm for Log-Linear Models	FAQ Segmentation: McCallum et. al
• Define <i>n</i> to be the length of the sentence • Define a dynamic programming table $\pi[i, u, v] = \max_{a, v \text{ at position } i}$ • Our goal is to calculate $\max_{u,v \in T} \pi[n, u, v]$ 37 39 The Viterbi Algorithm: Recursive Definitions • Base case: $\pi[0, u, v] = \log 1 = 0$ $\pi[0, u, v] = \log 0 = -\infty$ for all other u, v here * is a special tag padding the beginning of the sentence. • Recursive case: for $i = 1,, n$, for all u, v , $\pi[i, u, v] = \max_{i \in T \cup \{s\}} \{\pi[i - 1, t, u] + Score(S, i, t, u, v)\}$ • Recursive case: Here follows a diagram of the necessary connections $(\operatorname{canswery} (\operatorname{canswery} (cans$		1 0 00
$\pi[i, u, v] = \max \max \log \operatorname{constant}^{1}$ o Our goal is to calculate $\max_{u,v \in T} \pi[n, u, v]$ $37 \qquad 39$ The Viterbi Algorithm: Recursive Definitions $\operatorname{FAQ} \operatorname{Segmentation: McCallum et. al}$ $\pi[0, *, *] = \log 1 = 0$ $\pi[0, u, v] = \log 0 = -\infty \text{ for all other } u, v$ here * is a special tag padding the beginning of the sentence. $\operatorname{Recursive case: for i = 1 \dots n, for all u, v,$ $\pi[i, u, v] = \max_{t \in T\cup\{*\}} \{\pi[i - 1, t, u] + Score(S, i, t, u, v)\}$ $\operatorname{Horitout in this containt}^{1}$	• Define n to be the length of the sentence	
in tags u, v at position i • Our goal is to calculate $\max_{u,v \in T} \pi[n, u, v]$ 37 39 The Viterbi Algorithm: Recursive Definitions • Base case: $\pi[0, *, *] = \log 1 = 0$ $\pi[0, u, v] = \log 0 = -\infty$ for all other u, v here $*$ is a special tag padding the beginning of the sentence. • Recursive case: for $i = 1 \dots n$, for all u, v , $\pi[i, u, v] = \max_{t \in T \cup \{*\}} \{\pi[i - 1, t, u] + Score(S, i, t, u, v)\}$ $\pi[i, u, v] = \max_{t \in T \cup \{*\}} \{\pi[i - 1, t, u] + Score(S, i, t, u, v)\}$ $\pi[i, u, v] = \max_{t \in T \cup \{*\}} \{\pi[i - 1, t, u] + Score(S, i, t, u, v)\}$ $\pi[v, u, v] = \max_{t \in T \cup \{*\}} \{\pi[i - 1, t, u] + Score(S, i, t, u, v)\}$ $\pi[v, u, v] = \max_{t \in T \cup \{*\}} \{\pi[i - 1, t, u] + Score(S, i, t, u, v)\}$ $\pi[v, u, v] = \max_{t \in T \cup \{*\}} \{\pi[i - 1, t, u] + Score(S, i, t, u, v)\}$ $\pi[v, u, v] = \max_{t \in T \cup \{*\}} \{\pi[i - 1, t, u] + Score(S, i, t, u, v)\}$ $\pi[v, u, v] = \max_{t \in T \cup \{*\}} \{\pi[v, v] + Score(S, i, t, u, v)\}$	• Define a dynamic programming table	is difficult in this domain
37		
The Viterbi Algorithm: Recursive Definitions• Base case: $\pi[0, *, *] = \log 1 = 0$ $\pi[0, u, v] = \log 0 = -\infty$ for all other u, v here $*$ is a special tag padding the beginning of the sentence.• Recursive case: for $i = 1 \dots n$, for all u, v , $\pi[i, u, v] = \max_{t \in T \cup \{*\}} \{\pi[i - 1, t, u] + Score(S, i, t, u, v)\}$ • Chead>X-NNTP-POSTER: NewsHound v1.33 <head><head><head><head><head><head><head><head><head><head><head><head>head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><head><</head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head></head>	• Our goal is to calculate $\max_{u,v\in\mathcal{T}}\pi[n,u,v]$	
• Base case: $\pi[0, *, *] = \log 1 = 0$ $\pi[0, u, v] = \log 0 = -\infty \text{ for all other } u, v$ here * is a special tag padding the beginning of the sentence. • Recursive case: for $i = 1 \dots n$, for all u, v , $\pi[i, u, v] = \max_{t \in T \cup \{*\}} \{\pi[i - 1, t, u] + Score(S, i, t, u, v)\}$ $FAQ Segmentation: McCallum et. al Sequence of the sentence o$	37	39
$\pi[0, u, v] = \log 0 = -\infty \text{ for all other } u, v$ $here * \text{ is a special tag padding the beginning of the sentence.}$ $\bullet \text{ Recursive case: for } i = 1 \dots n, \text{ for all } u, v,$ $\pi[i, u, v] = \max_{t \in T \cup \{*\}} \{\pi[i - 1, t, u] + Score(S, i, t, u, v)\}$ $< \text{ chead} > chea$		FAQ Segmentation: McCallum et. al
$\pi[i, u, v] = \max_{t \in T \cup \{*\}} \{\pi[i-1, t, u] + Score(S, i, t, u, v)\}$ (answer> (answer> Here follows a diagram of the necessary connections (answer> Here follows a diagram of the necessary connections (answer> programs to work properly. They are as far as I know t (answer>agreed upon by commercial comms software developers for	$\pi[0, u, v] = \log 0 = -\infty$ for all other u, v here $*$ is a special tag padding the beginning of the sentence.	<head> <head>Archive name: acorn/faq/part2 <head>Frequency: monthly <head></head></head></head></head>
		<answer> <answer> Here follows a diagram of the necessary connections <answer>programs to work properly. They are as far as I know t</answer></answer></answer>

<answer>

<answer>

Backpointers allow us to recover the max probability sequence:

 $\mathbf{BP}[i, u, v] \quad = \quad \operatorname{argmax}_{t \in \mathcal{T} \cup \{ \ast \}} \left\{ \pi[i - 1, t, u] + Score(S, i, t, u, v) \right\}$

Where $Score(S, i, t, u, v) = \log P(v \mid t, u, w_1, \dots, w_n, i)$

Identical to Viterbi for HMMs, except for the definition of Score(S, i, t, u, v)

Pins 1, 4, and 8 must be connected together inside

<answer>is to avoid the well known serial port chip bugs. The

FAQ Segmentation: Line Features	
<pre>begins-with-number begins-with-ordinal begins-with-punctuation begins-with-question-word begins-with-subject blank contains-alphanum contains-bracketed-number contains-bracketed-number contains-bracketed-number contains-non-space contains-non-space contains-number contains-number contains-number contains-pipe contains-question-mark ends-with-question-mark first-alpha-is-capitalized indented-1-to-4 indented-1-to-4 indented-5-to-10 more-than-one-third-space only-punctuation</pre>	<pre>FAQ Segmentation: An HMM Tagger </pre> <pre><question>2.6) What configuration of serial cable should I use </question></pre> <pre>• First solution for P(word tag): P('2.6) What configuration of serial cable should I use" question) = P(2.6) question)× P(What question)× P(what question)× P(configuration question)× P(of question)× P(serial question)× </pre> • i.e. have a language model for each tag
prev-is-blank prev-begins-with-ordinal shorter-than-30	
41	43
FAQ Segmentation: The Log-Linear Tagger	FAQ Segmentation: McCallum et. al
<pre><head>X-NNTP-POSTER: NewsHound v1.33 <head></head></head></pre>	 Second solution: first map each sentence to string of features: <question>2.6) What configuration of serial cable should I use</question> ⇒ <question>begins-with-number contains-alphanum contains-nonspace</question> Use a language model again: P(*2.6) What configuration of serial cable should I use" question) = P(begins-with-number question)× P(contains-alphanum question)× P(contains-nonspace question)× P(contains-number question)× P(contains-number question)× P(contains-number question)× P(prev-is-blank question)×

FAQ Segmentation: Results

Method	Precision	Recall
ME-Stateless	0.038	0.362
TokenHMM	0.276	0.140
FeatureHMM	0.413	0.529
MEMM	0.867	0.681

- Precision and recall results are for recovering segments
- ME-stateless is a log-linear model that treats every sentence seperately (no dependence between adjacent tags)
- TokenHMM is an HMM with first solution we've just seen
- FeatureHMM is an HMM with second solution we've just seen
- MEMM is a log-linear trigram tagger (MEMM stands for 'Maximum-Entropy Markov Model')

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Overview

- The Tagging Problem
- Hidden Markov Model (HMM) taggers
- Log-linear taggers
- Log-linear models for parsing and other problems

Log-Linear Taggers: Summary

- The input sentence is $S = w_1 \dots w_n$
- Each tag sequence T has a conditional probability

$$P(T \mid S) = \prod_{j=1}^{n} P(t_j \mid w_1 \dots w_n, t_1 \dots t_{j-1})$$
 Chain rule

- $=\prod_{j=1}^{n} P(t_j \mid w_1 \dots w_n, t_{j-2}, t_{j-1})$ Independence assumptions
- Estimate $P(t_j | w_1 \dots w_n, t_{j-2}, t_{j-1})$ using log-linear models
- Use the Viterbi algorithm to compute

$$\operatorname{argmax}_{T \in \mathcal{T}^n} \log P(T \mid S)$$

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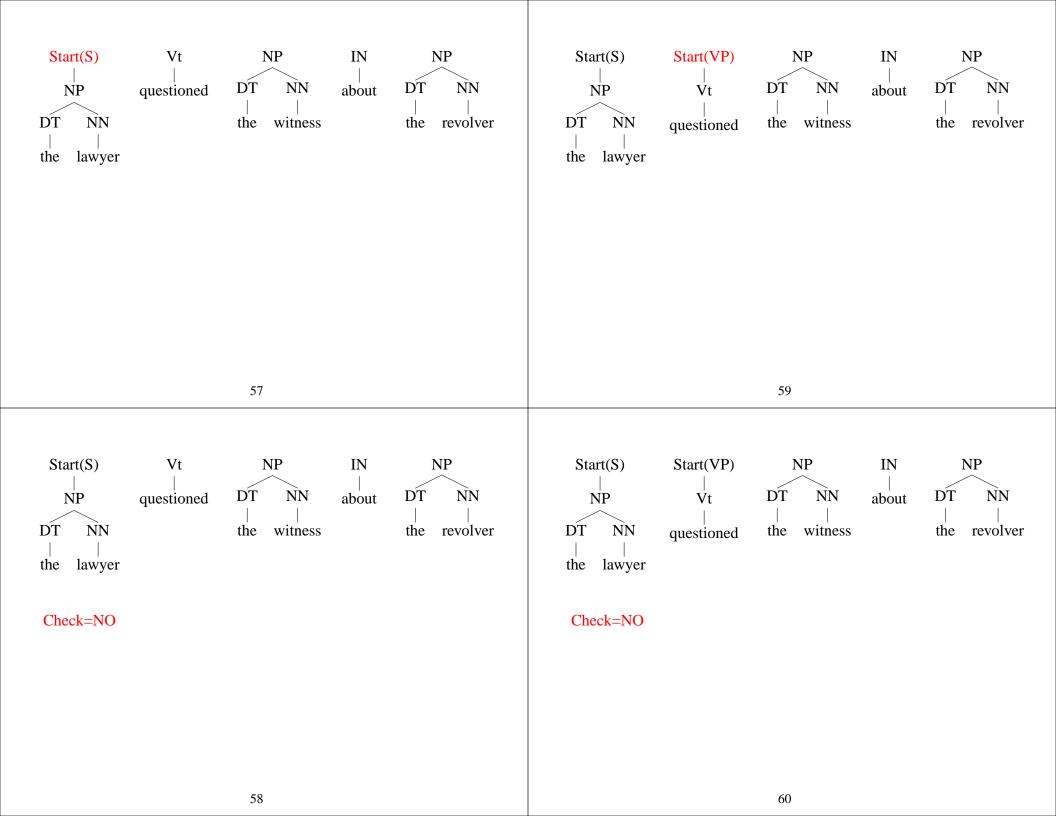
A General Approach: (Conditional) History-Based Models

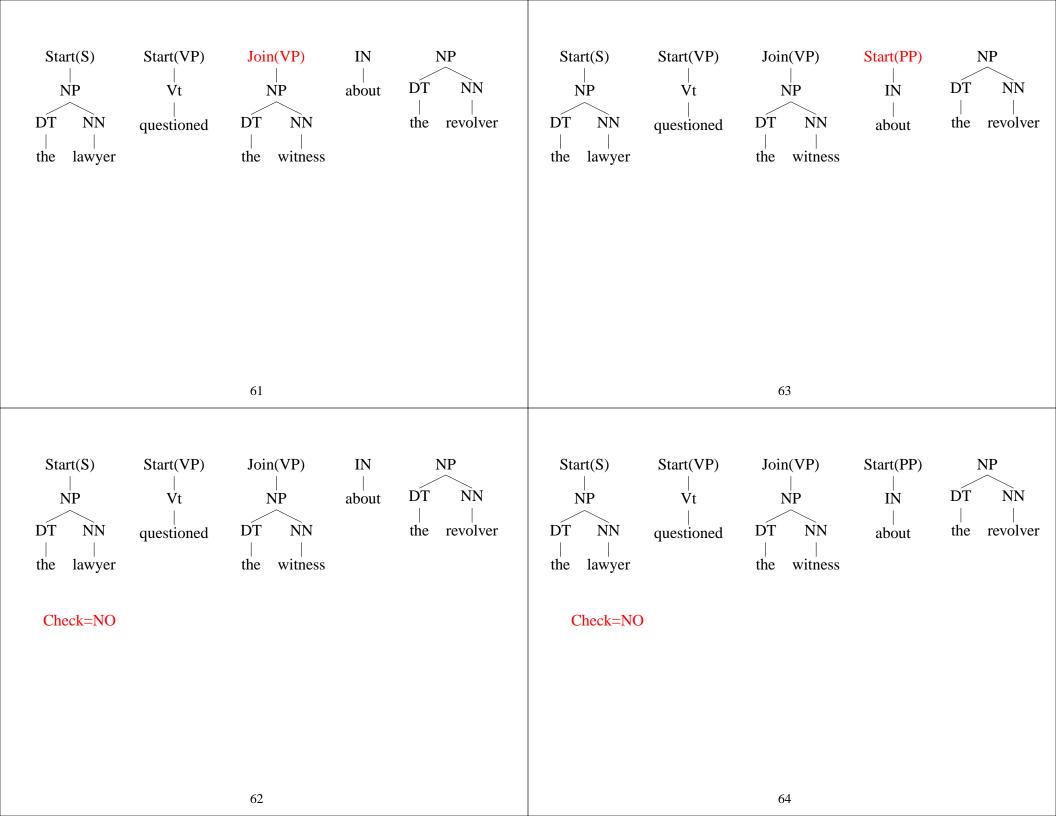
- We've shown how to define $P(T \mid S)$ where T is a tag sequence
- How do we define $P(T \mid S)$ if T is a parse tree (or another structure)?

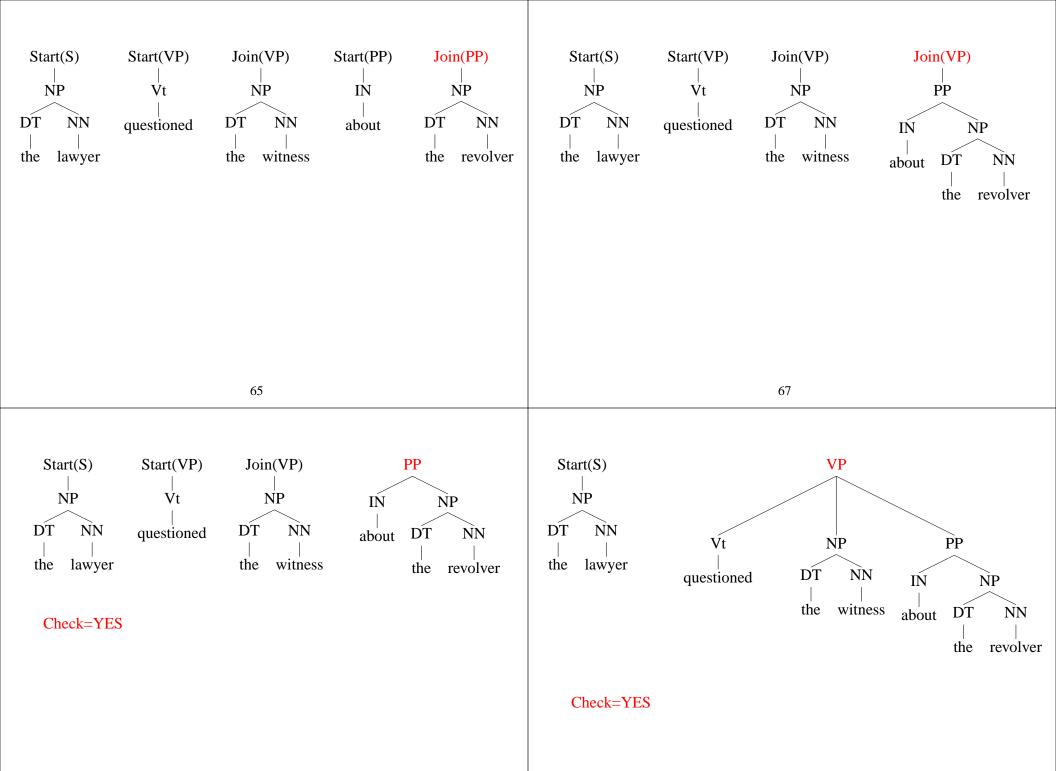
General Approach: (Conditional) History-Based Models	Ratnaparkhi's Parser: Three Layers of Structure
 Step 1: represent a tree as a sequence of decisions d₁d_m T = ⟨d₁, d₂,d_m⟩ m is not necessarily the length of the sentence Step 2: the probability of a tree is P(T S) = ∏^m_{i=1} P(d_i d₁d_{i-1}, S) Step 3: Use a log-linear model to estimate P(d_i d₁d_{i-1}, S) Step 4: Search?? (answer we'll get to later: beam or heuristic search) 	 Part-of-speech tags Chunks Remaining structure
49	51
An Example Tree S(questioned) NP(lawyer) DT NN the lawyer Vt NP(witness) Vt NP(witness) UT NN the witness about DT NN the witness about DT NN the revolver	Layer 1: Part-of-Speech Tags DT NN Vt DT NN IN DT NN I
50	52

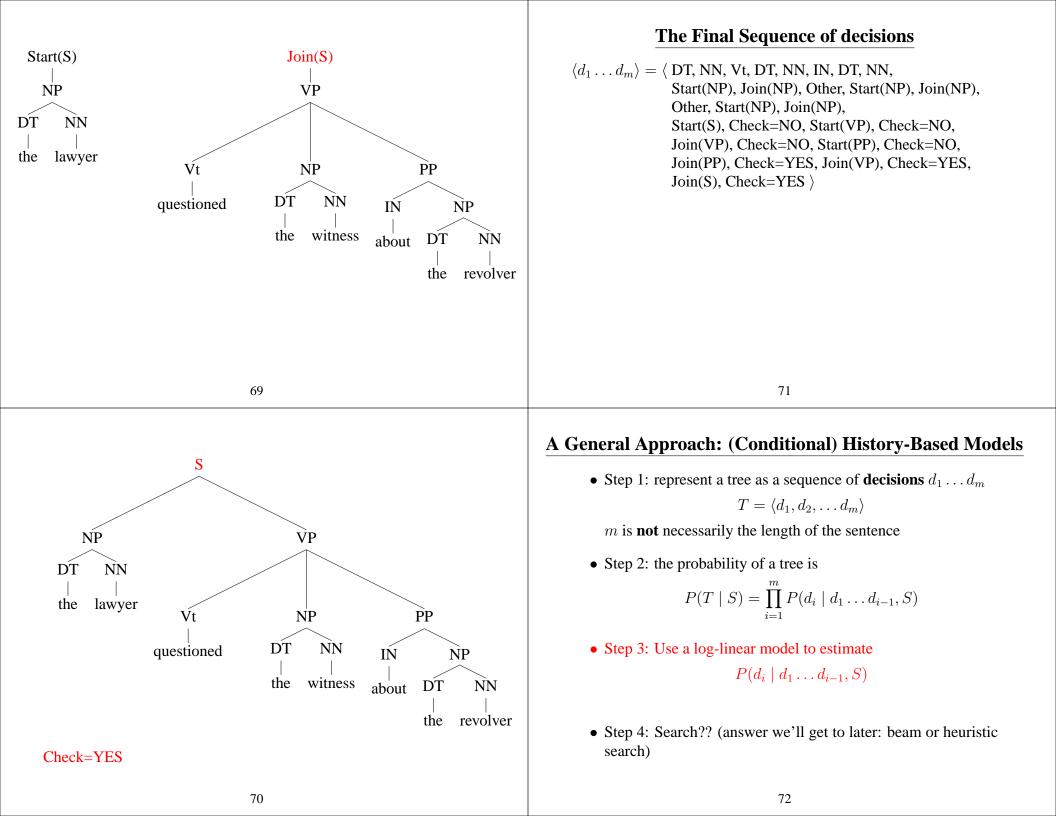
Α

Layer 2: Chunks	Layer 3: Remaining Structure Alternate Between Two Classes of Actions:
$\frac{NP}{DT} + \frac{Vt}{NN} + \frac{NP}{DT} + \frac{NP}{DT} + \frac{NP}{NN} + \frac{NP}{DT} + NP$	 Anternate Between Two Classes of Actions: Join(X) or Start(X), where X is a label (NP, S, VP etc.) Check=YES or Check=NO Meaning of these actions: Start(X) starts a new constituent with label X (always acts on leftmost constituent with no start or join label above it) Join(X) continues a constituent with label X (always acts on leftmost constituent with label X (always acts on leftmost constituent with label X (always acts on leftmost constituent with no start or join label above it) Check=NO does nothing Check=YES takes previous Join or Start action, and converts it into a completed constituent
53	55
Layer 2: ChunksStart(NP)Join(NP)OtherStart(NP)Join(NP)OtherStart(NP)Join(NP) DT NN Vt DT NN IN DT NN DT NN Vt DT NN IN DT NN He $Iawyer$ $questioned$ He $witness$ $about$ He $revolver$ • Step 1: represent a tree as a sequence of decisions $d_1 \dots d_n$	NP Vt NP IN NP DT NN questioned DT NN about DT NN the lawyer the witness the revolver
• Step 1. represent a free as a sequence of decisions $a_1 \dots a_n$ $T = \langle d_1, d_2, \dots d_n \rangle$	
• First <i>n</i> decisions are tagging decisions Next <i>n</i> decisions are chunk tagging decisions $\langle d_1 \dots d_{2n} \rangle = \langle \text{DT}, \text{NN}, \text{Vt}, \text{DT}, \text{NN}, \text{IN}, \text{DT}, \text{NN}, \text{Start}(\text{NP}), \text{Join}(\text{NP}), \text{Other, Start}(\text{NP}), \text{Join}(\text{NP}), \text{Join}(\text{NP}), \text{Other, Start}(\text{NP}), \text{Join}(\text{NP}) \rangle$	









Applying a Log-Linear Model

• Step 3: Use a log-linear model to estimate

$$P(d_i \mid d_1 \dots d_{i-1}, S)$$

• A reminder:

$$P(d_i \mid d_1 \dots d_{i-1}, S) = \frac{e^{\mathbf{f}(\langle d_1 \dots d_{i-1}, S \rangle, d_i) \cdot \mathbf{v}}}{\sum_{d \in \mathcal{A}} e^{\mathbf{f}(\langle d_1 \dots d_{i-1}, S \rangle, d) \cdot \mathbf{v}}}$$

where:

 $\begin{array}{lll} \langle d_1 \dots d_{i-1}, S \rangle & \quad \text{is the history} \\ & d_i & \quad \text{is the outcome} \\ & \mathbf{f} & \quad \text{maps a history/outcome pair to a feature vector} \\ & \mathbf{v} & \quad \text{is a parameter vector} \end{array}$

 \mathcal{A} is set of possible actions

Layer 3: Join or Start

- Looks at head word, constituent (or POS) label, and start/join annotation of *n*'th tree relative to the decision, where n = -2, -1
- Looks at head word, constituent (or POS) label of n'th tree relative to the decision, where n = 0, 1, 2
- Looks at bigram features of the above for (-1,0) and (0,1)
- Looks at trigram features of the above for (-2,-1,0), (-1,0,1) and (0, 1, 2)
- The above features with all combinations of head words excluded
- Various punctuation features

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Layer 3: Check=NO or Check=YES

• A variety of questions concerning the proposed constituent

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Applying a Log-Linear Model

• Step 3: Use a log-linear model to estimate

$$P(d_i \mid d_1 \dots d_{i-1}, S) = \frac{e^{\mathbf{f}(\langle d_1 \dots d_{i-1}, S \rangle, d_i) \cdot \mathbf{v}}}{\sum_{d \in \mathcal{A}} e^{\mathbf{f}(\langle d_1 \dots d_{i-1}, S \rangle, d) \cdot \mathbf{v}}}$$

- The big question: how do we define f?
- Ratnaparkhi's method defines **f** differently depending on whether next decision is:
 - A tagging decision (same features as before for POS tagging!)
 - A chunking decision
 - A start/join decision after chunking
 - A check=no/check=yes decision

The Search Problem

• In POS tagging, we could use the Viterbi algorithm because

 $P(t_j \mid w_1 \dots w_n, j, t_1 \dots t_{j-1}) = P(t_j \mid w_1 \dots w_n, j, t_{j-2} \dots t_{j-1})$

- Now: Decision d_i could depend on arbitrary decisions in the "past" \Rightarrow no chance for dynamic programming
- Instead, Ratnaparkhi uses a beam search method

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