Complete the following problems. Be sure to show your work for partial credit.

- 1. Mano and Kime 1-11.
- 2. Prove the following *consensus* theorem true, once using a truth table and once through algebraic manipulation:  $(X \cdot Y) + (Y \cdot Z) + (\overline{X} \cdot Z) = (X \cdot Y) + (\overline{X} \cdot Z)$
- 3. Mano and Kime 2-7.
- 4. Mano and Kime 2-8.
- 5. Design a majority circuit. This circuit has three inputs, A, B, and C. Its output, F is true if two or more of the inputs are true and is false otherwise.
  - (a) List a truth table for the majority circuit.
  - (b) Express F as a SOP.
  - (c) Minimize F using algebraic manipulation.
  - (d) Draw the schematic (circuit diagram) for the minimized F.
- 6. Mano and Kime 2-12.