

Computer Graphics (Spring 2008)

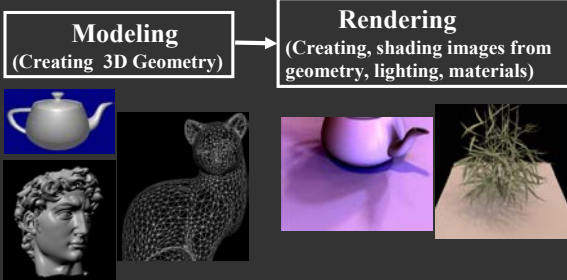
COMS 4160, Lecture 15: Illumination and Shading
<http://www.cs.columbia.edu/~cs4160>

To Do

- Work on HW 3, do well
- Start early on HW 4

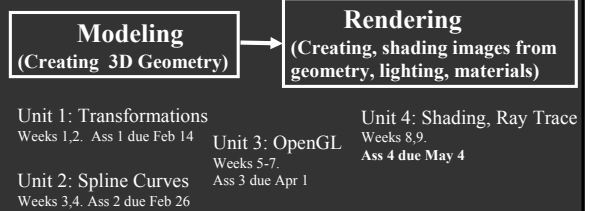
Course Outline

- 3D Graphics Pipeline



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Unit 1: Transformations
Weeks 1,2. Ass 1 due Feb 14

Unit 2: Spline Curves
Weeks 3,4. Ass 2 due Feb 26

Unit 3: OpenGL
Weeks 5-7.
Ass 3 due Apr 1

Unit 4: Shading, Ray Trace
Weeks 8,9.
Ass 4 due May 4

Midterm on units 1-3: Mar 10

Rendering: 1960s (visibility)

- Roberts (1963), Appel (1967) - hidden-line algorithms
- Warnock (1969), Watkins (1970) - hidden-surface
- Sutherland (1974) - visibility = sorting



Images from FvDFH, Pixar's Shutterbug
Slide ideas for history of Rendering: courtesy Marc Levoy

Rendering: 1970s (lighting)

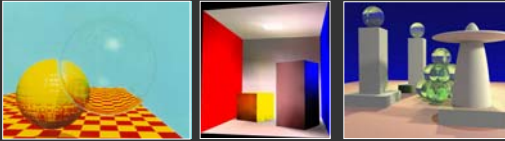
- 1970s - raster graphics
- Gouraud (1971) - diffuse lighting, Phong (1974) - specular lighting
- Blinn (1974) - curved surfaces, texture
- Catmull (1974) - Z-buffer hidden-surface algorithm



Rendering (1980s, 90s: Global Illumination)

early 1980s - global illumination

- Whitted (1980) - ray tracing
- Goral, Torrance et al. (1984) radiosity
- Kajiya (1986) - the rendering equation



Outline

- Preliminaries
- Basic diffuse and Phong shading
- Gouraud, Phong interpolation, smooth shading
- Formal reflection equation

For today's lecture, slides and chapter 9 in textbook

Motivation

- Objects not flat color, perceive shape with appearance
- Materials interact with lighting
- Compute correct shading pattern based on lighting
 - This is not the same as shadows (separate topic)
- Some of today's lecture review of last OpenGL lec.
 - Idea is to discuss illumination, shading independ. OpenGL
- Today, initial hacks (1970-1980)
 - Next lecture: formal notation and physics

Linear Relationship of Light

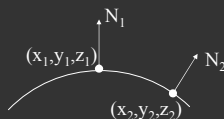
- Light energy is simply sum of all contributions

$$I = \sum_k I_k$$

- Terms can be calculated separately and later added together:
 - multiple light sources
 - multiple interactions (diffuse, specular, more later)
 - multiple colors (R-G-B, or per wavelength)

General Considerations

Surfaces are described as having a position, and a normal at every point.

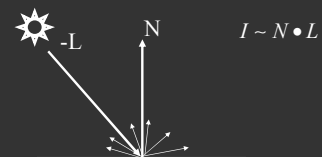


Other vectors used

- L = vector to the light source
light position minus surface point position
- E = vector to the viewer (eye)
viewer position minus surface point position

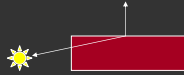
Diffuse Lambertian Term

- Rough matte (technically Lambertian) surfaces
 - Not shiny: matte paint, unfinished wood, paper, ...
- Light reflects equally in all directions
- Obey Lambert's cosine law
 - Not exactly obeyed by real materials

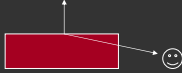


Meaning of negative dot products

- If $(N \cdot L)$ is negative, then the light is behind the surface, and cannot illuminate it.



- If $(N \cdot E)$ is negative, then the viewer is looking at the underside of the surface and cannot see it's front-face.



- In both cases, I is clamped to Zero.

Phong Illumination Model

- Specular or glossy materials: highlights
 - Polished floors, glossy paint, whiteboards
 - For plastics highlight is color of light source (not object)
 - For metals, highlight depends on surface color
- Really, (blurred) reflections of light source

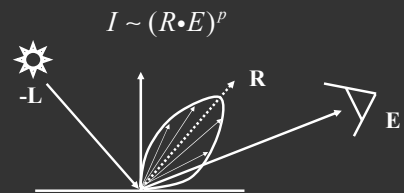


Roughness →

Idea of Phong Illumination

- Find a simple way to create highlights that are view-dependent and happen at about the right place
- Not physically based
- Use dot product (cosine) of eye and reflection of light direction about surface normal
- Alternatively, dot product of half angle and normal
- Raise cosine lobe to some power to control sharpness or roughness

Phong Formula

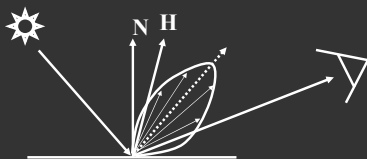


$$R = ?$$

$$R = -L + 2(L \cdot N)N$$

Alternative: Half-Angle (Blinn-Phong)

$$I \sim (N \cdot H)^p$$



- In practice, both diffuse and specular components for most materials

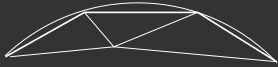
Outline

- Preliminaries
- Basic diffuse and Phong shading
- *Gouraud, Phong interpolation, smooth shading*
- Formal reflection equation

Not in text. If interested, look at FvDFH pp 736-738

Triangle Meshes as Approximations

- Most geometric models are large collections of triangles.
- Triangles have 3 vertices, each with a position, color, normal, and other parameters (such as n for Phong reflection).
- The triangles are an approximation to the actual surface of the object.



Vertex Shading

- We know how to calculate the light intensity given:
 - surface position
 - normal
 - viewer position
 - light source position (or direction)
- 2 ways for a vertex to get its normal:
 - given when the vertex is defined.
 - take all the normals from faces that share the vertex, and average them.

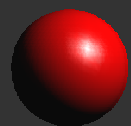
Coloring Inside the Polygon

- How do we shade a triangle between its vertices, where we aren't given the normal?
- Inter-vertex interpolation can be done in object space (along the face), but it is simpler to do it in image space (along the screen).

Flat vs. Gouraud Shading



`glShadeModel(GL_FLAT)`

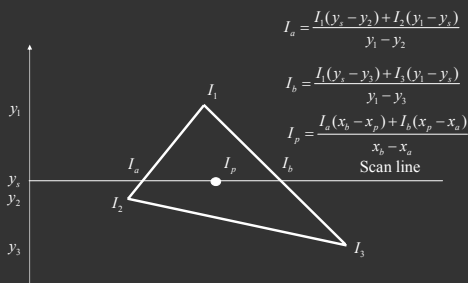


`glShadeModel(GL_SMOOTH)`

Flat - Determine that each face has a single normal, and color the entire face a single value, based on that normal.

Gouraud - Determine the color at each vertex, using the normal at that vertex, and interpolate linearly for the pixels between the vertex locations.

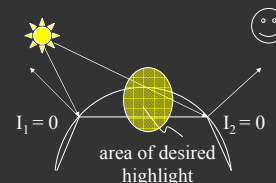
Gouraud Shading – Details



Actual implementation efficient: difference equations while scan converting

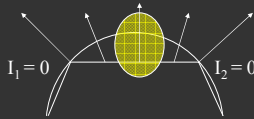
Gouraud and Errors

- $I_1 = 0$ because $(N \cdot E)$ is negative.
- $I_2 = 0$ because $(N \cdot L)$ is negative.
- Any interpolation of I_1 and I_2 will be 0.



2 Phongs make a Highlight

- Besides the Phong Reflectance model (\cos^n), there is a Phong Shading model.
- Phong Shading: Instead of interpolating the intensities between vertices, interpolate the **normals**.
- The entire lighting calculation is performed for each pixel, based on the interpolated normal. (OpenGL doesn't do this, but you can with current programmable shaders)



Problems with Interpolated Shading

- Silhouettes are still polygonal
- Interpolation in screen, not object space: perspective distortion
- Not rotation or orientation-independent
- How to compute vertex normals for sharply curving surfaces?
- But at end of day, polygons is mostly preferred to explicitly representing curved objects like spline patches for rendering

Outline

- Preliminaries
- Basic diffuse and Phong shading
- Gouraud, Phong interpolation, smooth shading
- Formal reflection equation*

Motivation

- Lots of ad-hoc tricks for shading
 - Kind of looks right, but?
- Physics of light transport
 - Will lead to formal reflection equation
- One of the more formal lectures
 - But important to solidify theoretical framework

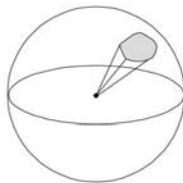
Angles and Solid Angles

■ **Angle** $\theta = \frac{l}{r}$

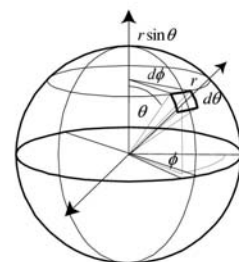
⇒ circle has 2π radians

■ **Solid angle** $\Omega = \frac{A}{R^2}$

⇒ sphere has 4π steradians



Differential Solid Angles



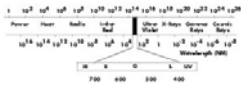
$$dA = (r d\theta)(r \sin \theta d\phi) = r^2 \sin \theta d\theta d\phi$$

$$d\omega = \frac{dA}{r^2} = \sin \theta d\theta d\phi$$

$$S = \int_0^{\pi} \int_0^{2\pi} \sin \theta d\theta d\phi = 4\pi$$

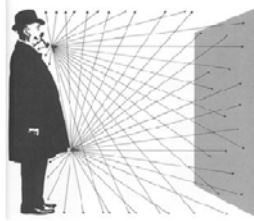
The Light Field

Electromagnetic waves and power spectrum



Ignore polarization
Ignore photons

Spatial distribution



From London and Upton

CS348B Lecture 4

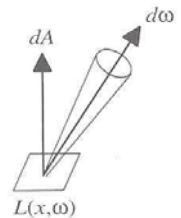
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Radiance

- Power per unit projected area perpendicular to the ray per unit solid angle in the direction of the ray

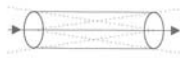
- Symbol: $L(x, \omega)$ ($\text{W}/\text{m}^2 \text{sr}$)

- Flux given by
 $d\Phi = L(x, \omega) \cos \theta d\omega dA$



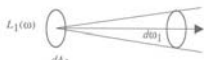
Radiance properties

- Radiance is constant as it propagates along ray
 - Derived from conservation of flux
 - Fundamental in Light Transport.



$$d\Phi_1 = L_1 d\omega_1 dA_1 = L_2 d\omega_2 dA_2 = d\Phi_2$$

$$d\omega_1 = dA_2 / r^2 \quad d\omega_2 = dA_1 / r^2$$



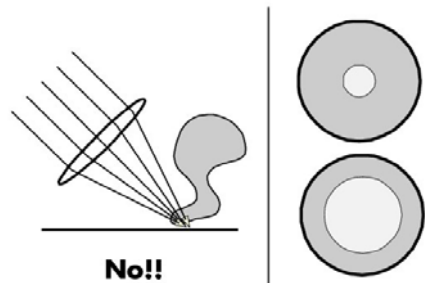
$$d\omega_1 dA_1 = \frac{dA_1 dA_2}{r^2} = d\omega_2 dA_2$$

$$\therefore L_1 = L_2$$



Quiz

Does radiance increase under a magnifying glass?

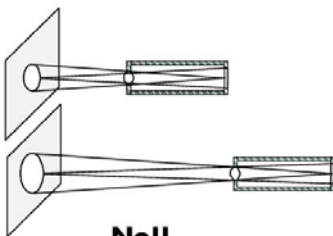


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Quiz

Does the brightness that a wall appears to the eye depend on the distance of the viewer to the wall?



No!!

CS348B Lecture 4

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Radiance properties

- Sensor response proportional to radiance (constant of proportionality is throughput)
 - Far away surface: See more, but subtends smaller angle
 - Wall equally bright across viewing distances
- Consequences
 - Radiance associated with rays in a ray tracer
 - Other radiometric quants derived from radiance

Irradiance, Radiosity

- Irradiance E is radiant power per unit area
- Integrate incoming radiance over hemisphere
 - Projected solid angle ($\cos \theta \, d\omega$)
 - Uniform illumination:
Irradiance = π [CW 24,25]
 - Units: W/m^2
- Radiosity
 - Power per unit area leaving surface (like irradiance)

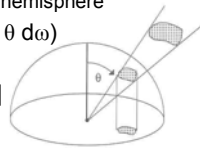


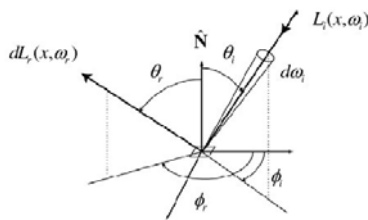
Figure 2.8: Projection of differential area.

Building up the BRDF

- Bi-Directional Reflectance Distribution Function [Nicodemus 77]
- Function based on incident, view direction
- Relates incoming light energy to outgoing light energy
- We have already seen special cases: Lambertian, Phong
- In this lecture, we study all this abstractly

The BRDF

Bidirectional Reflectance-Distribution Function



$$f_r(\omega_i \rightarrow \omega_r) \equiv \frac{dL_r(\omega_i \rightarrow \omega_r)}{dE_i} \left[\frac{1}{\text{sr}} \right]$$

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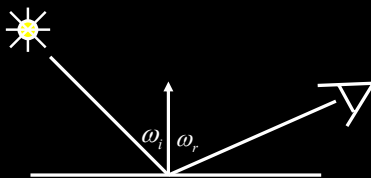
BRDF

- Reflected Radiance proportional to Irradiance
- Constant proportionality: BRDF [CW pp 28,29]
 - Ratio of outgoing light (radiance) to incoming light (irradiance)
 - Bidirectional Reflection Distribution Function
 - (4 Vars) units $1/\text{sr}$

$$f(\omega_i, \omega_r) = \frac{L_r(\omega_r)}{L_i(\omega_i) \cos \theta_i d\omega_i}$$

$$L_r(\omega_r) = L_i(\omega_i) f(\omega_i, \omega_r) \cos \theta_i d\omega_i$$

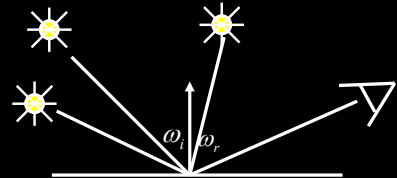
Reflection Equation



$$L_r(\omega_r) = L_i(\omega_i) f(\omega_i, \omega_r) (\omega_i \cdot n)$$

Reflected Radiance (Output Image) Incident radiance (from light source) BRDF Cosine of Incident angle

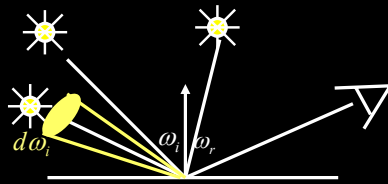
Reflection Equation



$$L_r(\omega_r) = \sum_i \text{Sum over all light sources} L_i(\omega_i) f(\omega_i, \omega_r) (\omega_i \cdot n)$$

Reflected Radiance (Output Image) Incident radiance (from light source) BRDF Cosine of Incident angle

Reflection Equation



$$L_r(\omega_r) = \int_{\Omega} \overset{\text{Replace sum with integral}}{L_i(\omega_i) f(\omega_i, \omega_r) (\omega_i \cdot n)} d\omega_i$$

$L_r(\omega_r)$: Reflected Radiance (Output Image)
 \int_{Ω} : Incident radiance (from light source)
 $f(\omega_i, \omega_r)$: BRDF
 $(\omega_i \cdot n)$: Cosine of Incident angle